

Trigonometry Worksheet: Trigonometric Equations (3)

Solve the trigonometric equation given by

$$\tan x \sin^2 x = 2 \tan x$$

$$\Rightarrow \tan x (\sin^2 x - 2) = 0$$

set each factor to zero and solve

$$\tan x = 0 \quad \text{and} \quad \sin^2(x) = 2$$

a) on the interval  $[0, \pi]$ ,  $\tan x = 0$  for  $x = 0$ .

and since the period of  $\tan x$  is  $\pi$ ,

the solutions are written as :

$$\begin{aligned}x &= 0 + k\pi \\x &= k\pi\end{aligned}$$

b)  $\sin^2(x) = 2$

$$\Rightarrow \sin(x) = \pm\sqrt{2}$$

this equation has no solutions

since  $-1 \leq \sin(x) \leq 1$ .